1. (15 points) (a) (4 points) Create a VHDL entity named `mux_16_to_1` that represents a 16 to 1 multiplexer. (b) (11 points) Create a VHDL architecture representing a structural model of the 16 to 1 mux using as many `mux_4_to_1` muxes as are needed. You do not need to write an entity or an architecture for `mux_4_to_1`. You may also assume that a component has already been declared and that no configuration statement is required.

```vhdl
entity MUX_16_TO_1 is
  port (I : in std_logic_vector(15 downto 0);
        SEL : in std_logic_vector(3 downto 0);
        O : out std_logic);
end MUX_16_TO_1;

architecture STRUCTURAL of MUX_16_TO_1 is
  component MUX_4_TO_1 is
    port (I : in std_logic_vector(3 downto 0);
          SEL : in std_logic_vector(1 downto 0);
          O : out std_logic);
  end component;

  signal INTERNAL : std_logic_vector(3 downto 0);

  U1 : MUX_4_TO_1
    port map(I => I(15 downto 12), SEL => SEL(1 downto 0),
             O => INTERNAL(3));

  U2 : MUX_4_TO_1
    port map(I => I(11 downto 8), SEL => SEL(1 downto 0),
             O => INTERNAL(2));

  U3 : MUX_4_TO_1
    port map(I => I(7 downto 4), SEL => SEL(1 downto 0),
             O => INTERNAL(1));

  U4 : MUX_4_TO_1
    port map(I => I(3 downto 0), SEL => SEL(1 downto 0),
             O => INTERNAL(0));

  U5 : MUX_4_TO_1
    port map(I(3) => INTERNAL(3), I(2) => INTERNAL(2),
             I(1) => INTERNAL(1), I(0) => INTERNAL(0),
             SEL => SEL(3 downto 2), O => O);
end STRUCTURAL;
```

2. (1 point) The synthesizable subset of VHDL is standard. (True/False) __False__

3. (20 points) (a) (12 points) Write a VHDL function that will take two integer vectors, A and B, and find the dot product \( C = \sum a_i * b_i \). The function call should be of the form `DOT(A, B)`, where A and B are integer vector signals. Use attributes inside the function to determine the length and range of the vectors. Make no assumptions about the high and low values of the ranges. For example, \( A(3 \text{ downto } 1) = (1,2,3), B(3 \text{ downto } 1) = (4,5,6) \), \( C = 3*6 + 2*5 + 1*4 = 32 \).

   \( A(0 \text{ to } 4) = (1,3,5,7,9), B(9 \text{ downto } 5) = (2,4,6,8,10) = 1*2 + 3*4 + 5*6 + 7*8 + 9*10 = 190 \)

   Output a warning if the ranges are not the same.

   (b) (8 points) Show an architecture that includes two calls to the function with the following properties. 1 - returns a value, 2 – triggers a warning message.
package MINE is
  type INTEGER_VECTOR is array (NATURAL RANGE <> ) of integer;
  function DOT_PRODUCT (L, R : INTEGER_VECTOR) return integer;
end MINE;

package BODY MINE is
  function DOT_PRODUCT (L, R : INTEGER_VECTOR)
  return integer is
    variable TEMP : integer := 0;
    alias new_l : INTEGER_VECTOR(L'LENGTH -1 downto 0) is L;
    alias new_r : INTEGER_VECTOR(L'LENGTH -1 downto 0) is R;
    begin
      assert (L'LENGTH = R'LENGTH)
      report "Ranges of operands are not the same"
      severity WARNING;
      for I in new_l'RANGE loop
        TEMP := TEMP + new_l(I)*new_r(I);
      end loop;
      return TEMP;
    end DOT_PRODUCT;
end MINE;

entity DOT_PRODUCT_CALL is
end DOT_PRODUCT_CALL;
architecture CALL of DOT_PRODUCT_CALL is
  signal A : INTEGER_VECTOR(2 to 8) := (1,3,5,6,4,2,0);
  signal B : INTEGER_VECTOR(24 downto 18) := (1,2,3,4,5,6,7);
  signal C : INTEGER_VECTOR(52 to 55) := (1,3,5,6);
  signal D : integer;
  signal E : integer;
  begin
    D <= DOT_PRODUCT(A, B);
    E <= DOT_PRODUCT(A, C);
  end CALL;

4. (1 point) All processes are executed at initialization. (True/False) ___True___
5. (1 point) A ___procedure___ is used when you have multiple return values.
6. (4 points) Translate the following statement to an if-then-else statement:
   
   transmit <= signal_a when state = idle else
     signal_b when state = incoming else
     signal_c when state = outgoing else
     signal_d;

   if (state = idle) transmit <= signal_a;
   elsif (state = incoming) transmit <= signal_b;
   elsif (state = outgoing) transmit <= signal_c;
   else transmit <= signal_d;

7. (1 point) For every process, there is an equivalent concurrent statement. (True/False) _False_ 
8. (4 points) (a) (2 points) Specify a CLASSIFICATION enumeration data type that spells out the
   various classifications for undergraduate students.(b) (2 points) Write a variable declaration
   MY_CLASS that has a value equal to the rightmost element of the type.
type CLASSIFICATION is (FRESHMAN, SOPHOMORE, JUNIOR, SENIOR);
variable MY_CLASS : CLASSIFICATION := SENIOR;

9. (1 point) Multiple architectures can exist for a single entity. (True/False) _True_

10. (1 point) Multiple Choice: _a_ is the default delay in VHDL. (a) Inertial (b) Transport

11. (6 points) (a) (4 points) Write a declaration of an array that can be used to hold the student numbers of the students in this class. (b) (2 points) Initialize the first element of this array with your student number.

   type CLASS_ANUMBERS is array (0 to 15) of string(1 to 9);
   variable CPE_426_526 : CLASS_ANUMBERS (0 => A12345678, others => A00000000);

12. (20 points) Given the following VHDL, indicate all transactions and events. Give the values of A, B, C, D, E, and F each time a change occurs. Carry this out until no further change occurs.

   entity prob is
     port (D : inout bit);
   end prob;

   architecture PROB of prob is
     signal A, B, C, E, F : bit;
     begin
       process
         A <= '1' after 5 ns,
            '0' after 12 ns;
         wait;
       end process;

       P1: process (A, C)
       begin
         B <= A after 2 ns;
         E <= C after 7 ns;
       end process P1;

       C <= transport A and B
          after 6 ns;

       P2: process (C, E)
       begin
         F <= C or E after 4 ns;
       end process P2;

       D <= A or B or C or F after 1 ns;
     end PROB;

<table>
<thead>
<tr>
<th>Time</th>
<th>Event</th>
<th>Processes Triggered</th>
<th>Scheduled Transactions</th>
<th>Event?</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 ns</td>
<td>A 0→1</td>
<td>P1</td>
<td>B ‘1’ 7 ns</td>
<td>Y</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>E ‘0’ 12 ns</td>
<td>N</td>
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<td>C</td>
<td>N</td>
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<td>D</td>
<td>Y</td>
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<tr>
<td>6 ns</td>
<td>D 0→1</td>
<td>None</td>
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</tr>
<tr>
<td>7 ns</td>
<td>B 0→1</td>
<td>C</td>
<td>C ‘1’ 13 ns</td>
<td>Y</td>
</tr>
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<td></td>
<td></td>
<td>D</td>
<td>D ‘1’ 8 ns</td>
<td>N</td>
</tr>
<tr>
<td>12 ns</td>
<td>A 1→0</td>
<td>P1</td>
<td>B ‘0’ 14 ns</td>
<td>Y</td>
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<td>E ‘0’ 19 ns</td>
<td>N</td>
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<td></td>
<td></td>
<td>C</td>
<td>Y (append since transport)</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>D</td>
<td>N</td>
</tr>
<tr>
<td>13 ns</td>
<td>C 0→1</td>
<td>P1</td>
<td>B ‘0’ 15 ns</td>
<td>N (already have B ‘0’ 14 ns)</td>
</tr>
</tbody>
</table>
entity P_ENCODE is
  port (D : in std_logic_vector(3 downto 0);
        X, Y, V : out std_logic);
end P_ENCODE;

architecture CONCURRENT of P_ENCODE is
begin
  V <= '1' when (D(3) = '1') else '1' when (D(2) = '1') else
         '1' when (D(1) = '1') else '1' when (D(0) = '1') else '0' when (D = "0000") else 'Z';
  X <= '1' when (D(3) = '1') else '1' when (D(2) = '1') else '0' when (D(1) = '1') else '0' when (D(0) = '1') else 'Z';
  Y <= '1' when (D(3) = '1') else '0' when (D(2) = '1') else '0' when (D(1) = '1') else '0' when (D(0) = '1') else 'Z';
end CONCURRENT;

architecture SEQUENTIAL of P_ENCODE is
begin
  process(D)
    variable TEMP : std_logic_vector(2 downto 0);
  begin
    if (D(3) = '1') then TEMP := "111";
    elsif (D(2) = '1') then TEMP := "101";
    elsif (D(1) = '1') then TEMP := "011";
    elsif (D(0) = '1') then TEMP := "001";
    elsif (D = "0000") then TEMP := "ZZ0";
    else TEMP := "ZZZ";
  end if;
  X <= TEMP(2);
  Y <= TEMP(1);
  V <= TEMP(0);
  end process;
end SEQUENTIAL;
14. (10 points) Draw the state diagram for the following state machine. Is it a Moore machine or a Mealy machine? Moore

ENTITY state_machine IS
  PORT (sig_in : IN BIT; clk, rst : IN BIT;
         sig_out : OUT BIT);
END state_machine;

ARCHITECTURE state_machine OF state_machine IS
  TYPE state_type IS (a, b, c, d, e);
  SIGNAL current_state, next_state : state_type;
BEGIN
  PROCESS (sig_in, current_state)
  BEGIN
    sig_out <= '0';
    next_state <= c;
    CASE current_state
    WHEN a =>
      IF sig_in = '0' THEN
        next_state <= a;
        sig_out <= '1';
      ELSE
        next_state <= d;
        sig_out <= '1';
      END IF;
    WHEN b =>
      IF sig_in = '0' THEN
        next_state <= b;
      ELSE
        next_state <= c;
      END IF;
    WHEN c =>
      IF sig_in = '1' THEN
        sig_out <= '1';
        next_state <= a;
      ELSE
        next_state <= b;
      END IF;
    WHEN d =>
      IF sig_in = '0' THEN
        next_state <= e;
      END IF;
    WHEN e =>
      IF sig_in = '1' THEN
        next_state <= c;
      END IF;
    END CASE;
  END PROCESS;
  PROCESS (clk)
  BEGIN
    IF (rst = '0') then
      current_state <= a;
    ELSIF (clk'EVENT AND clk = '1') THEN
      current_state <= next_state;
    END IF;
  END PROCESS;
END state_machine;
15. (10 points) An M-N flip-flop responds to the falling clock edge as follows:

- If M = N = ‘0’, the flip-flop changes state.
- If M = ‘0’ and N = ‘1’, the flip-flop output is set to ‘1’.
- If M = ‘1’ and N = ‘0’, the flip-flop output is set to ‘0’.
- If M = N = ‘1’, no change of flip-flop state occurs.
- The flip-flop is cleared asynchronously if CLRn = ‘0’.

Write a complete module that implements an M-N flip-flop.

```vhdl
entity M_N_FF is
  port (M, N, CLRn, CLK : std_logic;
        Q, QB : out std_logic);
end M_N_FF;

architecture M_N_FF of M_N_FF is
  signal TEMP : std_logic;
begin
  process(CLRn, CLK)
  begin
    if (CLRn = '0') then
      TEMP <= '0';
    elsif (CLK'event and CLK = '0') then
      if (M = '1' and N = '1') then
        TEMP <= not TEMP;
      elsif (M = '0' and N = '1') then
        TEMP <= '1';
      elsif (M = '1' and N = '0') then
        TEMP <= '0';
      end if;
    end if;
  end process;
  Q <= TEMP;
  QB <= not TEMP;
end M_N_FF;
```