Parallel Computers

- Definition: “A parallel computer is a collection of processing elements that cooperate and communicate to solve large problems fast.”
  Almasi and Gottlieb, Highly Parallel Computing, 1989

- Questions about parallel computers:
  - How large a collection?
  - How powerful are processing elements?
  - How do they cooperate and communicate?
  - How are data transmitted?
  - What type of interconnection?
  - What are HW and SW primitives for programmer?
  - Does it translate into performance?
Why Multiprocessors?

- Collect multiple microprocessors together to improve performance beyond a single processor
  - Collecting several more effective than designing a custom processor
- Complexity of current microprocessors
  - Do we have enough ideas to sustain 1.5X/yr?
  - Can we deliver such complexity on schedule?
- Slow (but steady) improvement in parallel software (scientific apps, databases, OS)
- Emergence of embedded and server markets driving microprocessors in addition to desktops
  - Embedded functional parallelism, producer/consumer model
  - Server figure of merit is tasks per hour vs. latency

Flynn’s Taxonomy (1972)

- SISD (Single Instruction Single Data)
  - uniprocessors
- MISD (Multiple Instruction Single Data)
  - multiple processors on a single data stream;
- SIMD (Single Instruction Multiple Data)
  - same instruction is executed by multiple processors using different data
  - Adv.: simple programming model, low overhead, flexibility, all custom integrated circuits
  - Examples: Illiac-IV, CM-2
- MIMD (Multiple Instruction Multiple Data)
  - each processor fetches its own instructions and operates on its own data
  - Examples: Sun Enterprise 5000, Cray T3D, SGI Origin
  - Adv.: flexible, use off-the-shelf micros
  - MIMD current winner (< 128 processor MIMD machines)
MIMD

Why is it the choice for general-purpose multiprocessors
- Flexible
  - can function as single-user machines focusing on high-performance for one application,
  - multiprogrammed machine running many tasks simultaneously, or
  - some combination of these two
- Cost-effective: use off-the-shelf processors

Major MIMD Styles
- Centralized shared memory
  ("Uniform Memory Access" time or "Shared Memory Processor")
- Decentralized memory (memory module with CPU)

Centralized Shared-Memory Architecture

Small processor counts makes it possible
- that processors share one a single centralized memory
- to interconnect the processors and memory by a bus

- C - Cache
- M - Memory
- IO - Input/Output
**Distributed Memory Machines**

- Nodes include processor(s), some memory, typically some IO, and interface to an interconnection network

![Diagram of Distributed Memory Machines]

- **Pro:** Cost effective approach to scale memory bandwidth
- **Pro:** Reduce latency for accesses to local memory
- **Con:** Communication complexity

**Memory Architectures**

- **DSM (Distributed Shared Memory)**
  - physically separate memories can be addressed as one logically shared address space
    - the same physical address on two different processors refers to the same location in memory

- **Multicomputer**
  - the address space consists of multiple private address spaces that are logically disjoint and cannot be addressed by a remote processor
    - the same physical address on two different processors refers to two different locations in two different memories
Communication Models

- **Shared Memory**
  - Processors communicate with shared address space
  - Easy on small-scale machines
  - Advantages:
    • Model of choice for uniprocessors, small-scale MPs
    • Ease of programming
    • Lower latency
    • Easier to use hardware controlled caching

- **Message passing**
  - Processors have private memories, communicate via messages
  - Advantages:
    • Less hardware, easier to design
    • Focuses attention on costly non-local operations

- Can support either SW model on either HW base

Performance Metrics: Latency and Bandwidth

- **Bandwidth**
  - Need high bandwidth in communication
  - Match limits in network, memory, and processor
  - Challenge is link speed of network interface vs. bisection bandwidth of network

- **Latency**
  - Affects performance, since processor may have to wait
  - Affects ease of programming, since requires more thought to overlap communication and computation
  - Overhead to communicate is a problem in many machines

- **Latency Hiding**
  - How can a mechanism help hide latency?
  - Increases programming system burden
  - Examples: overlap message send with computation, prefetch data, switch to other tasks
Shared Address Model Summary

- Each processor can name every physical location in the machine
- Each process can name all data it shares with other processes
- Data transfer via load and store
- Data size: byte, word, ... or cache blocks
- Uses virtual memory to map virtual to local or remote physical
- Memory hierarchy model applies: now communication moves data to local processor cache (as load moves data from memory to cache)
  - Latency, BW, scalability when communicate?

Shared Address/Memory Multiprocessor Model

- Communicate via Load and Store
  - Oldest and most popular model
- Based on timesharing: processes on multiple processors vs. sharing single processor
- Process: a virtual address space and ~ 1 thread of control
  - Multiple processes can overlap (share), but ALL threads share a process address space
- Writes to shared address space by one thread are visible to reads of other threads
  - Usual model: share code, private stack, some shared heap, some private heap
SMP Interconnect

- Processors to Memory AND to I/O
- Bus based: all memory locations equal access time so SMP = “Symmetric MP”
  - Sharing limited BW as add processors, I/O

Message Passing Model

- Whole computers (CPU, memory, I/O devices) communicate as explicit I/O operations
  - Essentially NUMA but integrated at I/O devices vs. memory system
- Send specifies local buffer + receiving process on remote computer
- Receive specifies sending process on remote computer + local buffer to place data
  - Usually send includes process tag and receive has rule on tag: match 1, match any
  - Synch: when send completes, when buffer free, when request accepted, receive wait for send
- Send+receive => memory-memory copy, where each each supplies local address, AND does pairwise synchronization!
Advantages of Shared-Memory Communication Model

- Compatibility with SMP hardware
- Ease of programming when communication patterns are complex or vary dynamically during execution
- Ability to develop apps using familiar SMP model, attention only on performance critical accesses
- Lower communication overhead, better use of BW for small items, due to implicit communication and memory mapping to implement protection in hardware, rather than through I/O system
- HW-controlled caching to reduce remote comm. by caching of all data, both shared and private

Advantages of Message-passing Communication Model

- The hardware can be simpler (esp. vs. NUMA)
- Communication explicit => simpler to understand; in shared memory it can be hard to know when communicating and when not, and how costly it is
- Explicit communication focuses attention on costly aspect of parallel computation, sometimes leading to improved structure in multiprocessor program
- Synchronization is naturally associated with sending messages, reducing the possibility for errors introduced by incorrect synchronization
- Easier to use sender-initiated communication, which may have some advantages in performance
Amdahl’s Law and Parallel Computers

- Amdahl's Law (FracX: original % to be speed up)
  Speedup = 1 / [(FracX/SpeedupX + (1-FracX))]
- A portion is sequential => limits parallel speedup
  - Speedup <= 1/ (1-FracX)
- Ex. What fraction sequential to get 80X speedup from 100 processors? Assume either 1 processor or 100 fully used
  - 80 = 1 / [(FracX/100 + (1-FracX)]
  - 0.8*FracX + 80*(1-FracX) = 80 - 79.2*FracX = 1
  - FracX = (80-1)/79.2 = 0.9975
  - Only 0.25% sequential!

Small-Scale—Shared Memory

- Caches serve to:
  - Increase bandwidth versus bus/memory
  - Reduce latency of access
  - Valuable for both private data and shared data
- What about cache consistency?

<table>
<thead>
<tr>
<th>Time</th>
<th>Event</th>
<th>$A$</th>
<th>$B$</th>
<th>$X$ (memory)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td></td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>CPU A: R x</td>
<td>1</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>CPU B: R x</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>CPU A: W x,0</td>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
</tbody>
</table>
What Does Coherency Mean?

- Informally:
  - “Any read of a data item must return the most recently written value”
  - this definition includes both coherence and consistency
    - coherence: what values can be returned by a read
    - consistency: when a written value will be returned by a read

- Memory system is coherent if
  - a read(X) by P1 that follows a write(X) by P1, with no writes of X by another processor occurring between these two events, always returns the value written by P1
  - a read(X) by P1 that follows a write(X) by another processor, returns the written value if the read and write are sufficiently separated and no other writes occur between
  - writes to the same location are serialized: two writes to the same location by any two CPUs are seen in the same order by all CPUs

Potential HW Coherence Solutions

- Snooping Solution (Snoopy Bus):
  - every cache that has a copy of the data also has a copy of the sharing status of the block
  - Processors snoop to see if they have a copy and respond accordingly
  - Requires broadcast, since caching information is at processors
  - Works well with bus (natural broadcast medium)
  - Dominates for small scale machines (most of the market)

- Directory-Based Schemes (discuss later)
  - Keep track of what is being shared in 1 centralized place (logically)
  - Distributed memory => distributed directory for scalability (avoids bottlenecks)
  - Send point-to-point requests to processors via network
  - Scales better than Snooping
  - Actually existed BEFORE Snooping-based schemes
Basic Snoopy Protocols

- Write Invalidate Protocol
  - A CPU has exclusive access to a data item before it writes that item
  - Write to shared data: an invalidate is sent to all caches which snoop and invalidate any copies
  - Read Miss:
    - Write-through: memory is always up-to-date
    - Write-back: snoop in caches to find most recent copy

- Write Update Protocol (typically write through):
  - Write to shared data: broadcast on bus, processors snoop, and update any copies
  - Read miss: memory is always up-to-date

- Write serialization: bus serializes requests!
  - Bus is single point of arbitration

Write Invalidate versus Update

- Multiple writes to the same word with no intervening reads
  - Update: multiple broadcasts

- For multiword cache blocks
  - Update: each word written in a cache block requires a write broadcast
  - Invalidate: only the first write to any word in the block requires an invalidation

- Update has lower latency between write and read
Snooping Cache Variations

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Exclusive</td>
<td>Owned Exclusive</td>
<td>Private Dirty</td>
<td>Modified (private, ≠ Memory)</td>
</tr>
<tr>
<td></td>
<td>Owned Shared</td>
<td>Private Clean</td>
<td>exclusive (private, = Memory)</td>
</tr>
<tr>
<td></td>
<td>Shared</td>
<td>Shared</td>
<td>shared (shared, = Memory)</td>
</tr>
<tr>
<td></td>
<td>Invalid</td>
<td>Invalid</td>
<td>Invalid</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Owner can update via bus invalidate operation
Owner must write back when replaced in cache
If read sourced from memory, then Private Clean
if read sourced from other cache, then Shared
Can write in cache if held private clean or dirty

An Example Snoopy Protocol

- Invalidation protocol, write-back cache
- Each block of memory is in one state:
  - Clean in all caches and up-to-date in memory (Shared)
  - OR Dirty in exactly one cache (Exclusive)
  - OR Not in any caches
- Each cache block is in one state (track these):
  - Shared : block can be read
  - OR Exclusive : cache has only copy, its writeable, and dirty
  - OR Invalid : block contains no data
- Read misses: cause all caches to snoop bus
- Writes to clean line are treated as misses
### Snoopy-Cache State Machine-I

- **Invalid**
  - CPU Read
    - Place read miss on bus
- **Shared** (read/only)
  - CPU Read
    - Place read miss on bus
- **Exclusive** (read/write)
  - CPU Read
    - Place read miss on bus
  - CPU Write
    - Place Write Miss on Bus
- **CPU read hit**
- **CPU write hit**

### Snoopy-Cache State Machine-II

- **Invalid**
  - Write miss for this block
  - Write Back Block; (abort memory access)
- **Shared** (read/only)
  - Read miss for this block
    - Write Back Block; (abort memory access)
- **Exclusive** (read/write)
  - Write miss for this block
  - Write Back Block; (abort memory access)
Snoopy-Cache State Machine-III

State machine for CPU requests for each cache block and for bus requests for each cache block.

Cache Block State

Invalid

Write miss for this block
Write Back Block; (abort memory access)

Exclusive (read/write)

CPU read hit
CPU write hit

Shared (read/only)

Write miss for this block
Place read miss on bus

CPU Read miss

Write back block, Place read miss on bus
CPU Write

Write Back Block; (abort memory access)

CPU Write Miss

Write back cache block
Place write miss on bus

Remote Write

CPU Read hit

Write miss on bus

Remote Read

Write Back

CPU Write

Place Write Miss on Bus

Read miss

Write Back Block; (abort memory access)

CPU Write Miss

Write back cache block
Place write miss on bus

Remote Write

CPU Read hit

Write miss on bus

Remote Read

Write Back

CPU Write

Place Write Miss on Bus

Example

Processor 1 | Processor 2 | Bus | Memory
---|---|---|---
Step | State | Addr | Value | State | Addr | Value | Action | Proc | Addr | Value | Addr | Value
---|---|---|---|---|---|---|---|---|---|---|---|---
P1 | Write 10 to A1
P2 | Read A1
P2 | Read A1
P2 | Write 20 to A1
P2 | Write 40 to A2

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 != A2
Example: Step 1

<table>
<thead>
<tr>
<th>Step</th>
<th>P1 State</th>
<th>Addr</th>
<th>Value</th>
<th>P2 State</th>
<th>Addr</th>
<th>Value</th>
<th>Bus Action Proc</th>
<th>Addr</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Write 10 to A1</td>
<td>Excl</td>
<td>A1</td>
<td>10</td>
<td>Excl</td>
<td>A1</td>
<td>10</td>
<td>WrMs</td>
<td>P1</td>
</tr>
<tr>
<td>2</td>
<td>Read A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Read A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>Write 20 to A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>Write 40 to A2</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 != A2.

Active arrow =

Example: Step 2

<table>
<thead>
<tr>
<th>Step</th>
<th>P1 State</th>
<th>Addr</th>
<th>Value</th>
<th>P2 State</th>
<th>Addr</th>
<th>Value</th>
<th>Bus Action Proc</th>
<th>Addr</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Write 10 to A1</td>
<td>Excl</td>
<td>A1</td>
<td>10</td>
<td>Excl</td>
<td>A1</td>
<td>10</td>
<td>WrMs</td>
<td>P1</td>
</tr>
<tr>
<td>2</td>
<td>Read A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Read A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>Write 20 to A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>Write 40 to A2</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 != A2.
Example: Step 3

<table>
<thead>
<tr>
<th>Step</th>
<th>P1 State</th>
<th>Addr</th>
<th>Value</th>
<th>Bus Action</th>
<th>Proc Addr</th>
<th>Value</th>
<th>Memory Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>1:</td>
<td>Write 10 to A1</td>
<td>Excl.</td>
<td>A1</td>
<td>10</td>
<td>WrMs</td>
<td>P1</td>
<td>A1</td>
</tr>
<tr>
<td>2:</td>
<td>Read A1</td>
<td>Excl.</td>
<td>A1</td>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3:</td>
<td>Read A1</td>
<td>Share</td>
<td>A1</td>
<td>10</td>
<td>RdMs</td>
<td>P2</td>
<td>A1</td>
</tr>
<tr>
<td>4:</td>
<td>Share A1</td>
<td>10</td>
<td></td>
<td></td>
<td>WrBk</td>
<td>P1</td>
<td>A1</td>
</tr>
<tr>
<td>5:</td>
<td>Write 20 to A1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>6:</td>
<td>Write 40 to A2</td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
</tbody>
</table>

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 ≠ A2.

Example: Step 4

<table>
<thead>
<tr>
<th>Step</th>
<th>P1 State</th>
<th>Addr</th>
<th>Value</th>
<th>Bus Action</th>
<th>Proc Addr</th>
<th>Value</th>
<th>Memory Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>1:</td>
<td>Write 10 to A1</td>
<td>Excl.</td>
<td>A1</td>
<td>10</td>
<td>WrMs</td>
<td>P1</td>
<td>A1</td>
</tr>
<tr>
<td>2:</td>
<td>Read A1</td>
<td>Excl.</td>
<td>A1</td>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3:</td>
<td>Read A1</td>
<td>Share</td>
<td>A1</td>
<td>10</td>
<td>RdMs</td>
<td>P2</td>
<td>A1</td>
</tr>
<tr>
<td>4:</td>
<td>Share A1</td>
<td>10</td>
<td></td>
<td></td>
<td>WrBk</td>
<td>P1</td>
<td>A1</td>
</tr>
<tr>
<td>5:</td>
<td>Write 20 to A1</td>
<td>Inv.</td>
<td>A1</td>
<td>10</td>
<td>WrMs</td>
<td>P2</td>
<td>A1</td>
</tr>
<tr>
<td>6:</td>
<td>Write 40 to A2</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 ≠ A2.
Example: Step 5

<table>
<thead>
<tr>
<th>Step</th>
<th>Proc</th>
<th>Addr</th>
<th>Value</th>
<th>Action</th>
<th>Proc</th>
<th>Addr</th>
<th>Value</th>
<th>Proc</th>
<th>Addr</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1: Write 10 to A1</td>
<td>Excl</td>
<td>A1</td>
<td>10</td>
<td>WtMs</td>
<td>P1</td>
<td>A1</td>
<td>10</td>
<td>P2</td>
<td>A1</td>
<td>10</td>
</tr>
<tr>
<td>P1: Read A1</td>
<td>Excl</td>
<td>A1</td>
<td>10</td>
<td>WrBk</td>
<td>P1</td>
<td>A1</td>
<td>10</td>
<td>P2</td>
<td>A1</td>
<td>10</td>
</tr>
<tr>
<td>P2: Write 20 to A1</td>
<td>Inv</td>
<td>A1</td>
<td>10</td>
<td>WrMs</td>
<td>P2</td>
<td>A1</td>
<td>10</td>
<td>P2</td>
<td>A1</td>
<td>10</td>
</tr>
<tr>
<td>P2: Write 40 to A2</td>
<td>Excl</td>
<td>A2</td>
<td>40</td>
<td>WtMs</td>
<td>P2</td>
<td>A2</td>
<td>40</td>
<td>P2</td>
<td>A2</td>
<td>40</td>
</tr>
</tbody>
</table>

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 ≠ A2

Implementation Complications

- **Write Races:**
  - Cannot update cache until bus is obtained
  - Otherwise, another processor may get bus first, and then write the same cache block!
  - Two step process:
    - Arbitrate for bus
    - Place miss on bus and complete operation
  - If miss occurs to block while waiting for bus, handle miss (invalidate may be needed) and then restart
  - Split transaction bus:
    - Bus transaction is not atomic: can have multiple outstanding transactions for a block
    - Multiple misses can interleave, allowing two caches to grab block in the Exclusive state
    - Must track and prevent multiple misses for one block
- **Must support interventions and invalidations**
Implementing Snooping Caches

- Multiple processors must be on bus, access to both addresses and data
- Add a few new commands to perform coherency, in addition to read and write
- Processors continuously snoop on address bus
  - If address matches tag, either invalidate or update
- Since every bus transaction checks cache tags, could interfere with CPU just to check:
  - solution 1: duplicate set of tags for L1 caches just to allow checks in parallel with CPU
  - solution 2: L2 cache already duplicate, provided L2 obeys inclusion with L1 cache
    - block size, associativity of L2 affects L1

Implementing Snooping Caches

- Bus serializes writes, getting bus ensures no one else can perform memory operation
- On a miss in a write back cache, may have the desired copy and its dirty, so must reply
- Add extra state bit to cache to determine shared or not
- Add 4th state (MESI)
Fundamental Issues

- 3 Issues to characterize parallel machines
  - 1) Naming
  - 2) Synchronization
  - 3) Performance: Latency and Bandwidth
    (covered earlier)

Fundamental Issue #1: Naming

- Naming: how to solve large problem fast
  - what data is shared
  - how it is addressed
  - what operations can access data
  - how processes refer to each other

- Choice of naming affects code produced by a compiler; via load where just remember address or keep track of processor number and local virtual address for msg. passing

- Choice of naming affects replication of data; via load in cache memory hierarchy or via SW replication and consistency
Fundamental Issue #1: Naming

- Global physical address space: any processor can generate, address and access it in a single operation
  - memory can be anywhere: virtual addr. translation handles it
- Global virtual address space: if the address space of each process can be configured to contain all shared data of the parallel program
- Segmented shared address space: locations are named <process number, address> uniformly for all processes of the parallel program

Fundamental Issue #2: Synchronization

- To cooperate, processes must coordinate
- Message passing is implicit coordination with transmission or arrival of data
- Shared address => additional operations to explicitly coordinate: e.g., write a flag, awaken a thread, interrupt a processor
Summary: Parallel Framework

Layers:

- Programming Model:
  - Multiprogramming: lots of jobs, no communication
  - Shared address space: communicate via memory
  - Message passing: send and receive messages
  - Data Parallel: several agents operate on several data sets simultaneously and then exchange information globally and simultaneously (shared or message passing)

- Communication Abstraction:
  - Shared address space: e.g., load, store, atomic swap
  - Message passing: e.g., send, receive library calls
  - Debate over this topic (ease of programming, scaling) => many hardware designs 1:1 programming model

Distributed Directory MPs

C - Cache
M - Memory
IO - Input/Output

Interconnection Network
Directory Protocol

- Similar to Snoopy Protocol: Three states
  - Shared: ≥ 1 processors have data, memory up-to-date
  - Uncached (no processor has it; not valid in any cache)
  - Exclusive: 1 processor (owner) has data;
    memory out-of-date

- In addition to cache state, must track which processors have data when in the shared state
  (usually bit vector, 1 if processor has copy)

- Keep it simple(r):
  - Writes to non-exclusive data
    => write miss
  - Processor blocks until access completes
  - Assume messages received
    and acted upon in order sent

No bus and don’t want to broadcast:
- interconnect no longer single arbitration point
- all messages have explicit responses

Terms: typically 3 processors involved
- Local node where a request originates
- Home node where the memory location
  of an address resides
- Remote node has a copy of a cache
  block, whether exclusive or shared

Example messages on next slide:
P = processor number, A = address
Directory Protocol Messages

<table>
<thead>
<tr>
<th>Message type</th>
<th>Source</th>
<th>Destination</th>
<th>Msg Content</th>
</tr>
</thead>
<tbody>
<tr>
<td>Read miss</td>
<td>Local cache</td>
<td>Home directory</td>
<td>Processor P reads data at address A; make P a read sharer and arrange to send data back</td>
</tr>
<tr>
<td>Write miss</td>
<td>Local cache</td>
<td>Home directory</td>
<td>Processor P writes data at address A; make P the exclusive owner and arrange to send data back</td>
</tr>
<tr>
<td>Invalidate</td>
<td>Home directory</td>
<td>Remote caches</td>
<td>Invalidate a shared copy at address A.</td>
</tr>
<tr>
<td>Fetch</td>
<td>Home directory</td>
<td>Remote cache</td>
<td>Fetch the block at address A and send it to its home directory</td>
</tr>
<tr>
<td>Fetch/Invalidate</td>
<td>Home directory</td>
<td>Remote cache</td>
<td>Fetch the block at address A and send it to its home directory; invalidate the block in the cache</td>
</tr>
<tr>
<td>Data value reply</td>
<td>Home directory</td>
<td>Local cache</td>
<td>Return a data value from the home memory (read miss response)</td>
</tr>
<tr>
<td>Data write-back</td>
<td>Remote cache</td>
<td>Home directory</td>
<td>Write-back a data value for address A (invalidate response)</td>
</tr>
</tbody>
</table>

State Transition Diagram for an Individual Cache Block in a Directory Based System

- States identical to snoopy case; transactions very similar
- Transitions caused by read misses, write misses, invalidates, data fetch requests
- Generates read miss & write miss msg to home directory
- Write misses that were broadcast on the bus for snooping => explicit invalidate & data fetch requests
- Note: on a write, a cache block is bigger, so need to read the full cache block
CPU - Cache State Machine

- State machine for CPU requests for each memory block
- Invalid state if in memory
  send Data Write Back message to home directory

- CPU read hit / CPU write hit

Shared (read/only)

Invalid

Invalid state if in memory

CPU read miss: Send Read Miss
message to home directory

Fetch: send Data Write Back message to home directory

CPU read: Send Write Miss message to home directory

CPU Write: Send Write Miss message to home directory

CPU Write: Send Data Write Back message and Read Miss to home directory

CPU write miss: Send Data Write Back message and Write Miss to home directory

State Transition Diagram for the Directory

- Same states & structure as the transition diagram for an individual cache
- 2 actions: update of directory state & send msgs to satisfy requests
- Tracks all copies of memory block.
- Also indicates an action that updates the sharing set, Sharers, as well as sending a message.
Directory State Machine

- State machine for Directory requests for each memory block.
- Uncached state if in memory:
  - Data Write Back: Sharers = {} (Write back block)

Exclusive (read/writ)
- Write Miss: Sharers = {P}; send Fetch/Invalidate; send Data Value Reply msg to remote cache
- Read miss: Sharers += {P}; send Data Value Reply msg

Shared (read only)
- Write Miss: Send Invalidate to Sharers; then Sharers = {P}; send Data Value Reply msg
- Read miss: Sharers += {P}; send Data Value Reply msg

Uncached if in memory:
- Data Write Back: Sharers = {} (Write back block)